

Algebra & Equations Homework

REFERENCES:

Answers:

services.nietc.org

Khan Academy:

<https://www.khanacademy.org/math/algebra-home>

Math is Fun:

<https://www.mathsisfun.com/algebra/index.html>

Purple Math:

<http://www.purplemath.com/modules/solvein.htm>


NOTE: Subscripts (i.e. X_L , X_C) are used to differentiate between variables. These variables may have similar properties, but are still separate variables. For example: R_1 and R_2 will be used as variables for resistor #1 and resistor #2 in a circuit. Both are measured in Ohms but will likely have different values.

QUESTIONS:

1) Change the following rule into a formula:

The Power In Watts (P) In A Circuit Is Equal To The Voltage (E) Multiplied By The Current (I).


Answer:

- a. $I = P \times E$
- b. $E = I \times P$
-  c. $P = E \times I$
- d. $P = I \times E^2$

2) Change the following rule into a formula.

The Resistance In Ohms (R) In A Circuit Is Equal To The Voltage (E) Divided By The Current (I).


Answer:

- a. $E = I \div R$
- b. $I = E \div R$
- c. $R = I \div E$
-  d. $R = E \div I$

3) Find the value of the variable A in the equation: $A = \frac{BH}{2}$


If $B = 13$ And $H = 5$.

Answer:

- a. 30.2
-  b. 32.5
- c. 65
- d. 65.7

4) $A \times B = AB$ if $AB = 63$ and $B = 12.6$, what is the value of A?

Answer:

- e. $A = 3$
-  f. $A = 5$
- g. $A = 7$
- h. $A = 9$

5) How could someone prove he or she answered the previous question correctly?

Answer:

- i. Run the calculation(s) again to test the equation.
- j. Substitute any values into the original equation and verify the equality.
- k. Substitute the original values into the original equation and verify equality.
- l. Substitute the calculated values into the original equation and verify equality.

6) If a person multiplies one side of an equation by five, what must he or she do to the other side of the equation?

Answer:

- a. Add five.
- b. Divide by five.
- c. Multiply by five.
- d. Subtract five.

7) Solve the following equation: $15Y = 90$

Answer:

- a. $Y = 0.166$
- b. $Y = 5$
- c. $Y = 6$
- d. $Y = 9$

8) To solve $15Y = 90$, a person must ? each side of the equation by ?.

Answer:

- a. divide by 15
- b. divide by 90
- c. multiply by 15
- d. multiply by 90

9) Solve for R in the following equation: $\frac{R}{5} = 6$

Answer:

- a. 15
- b. 30
- c. 36
- d. 40

10) To solve $A + 17 = 20$, a person must ? each side of the equation.

Answer:

- a. add 17 to
- b. divide 17 on
- c. multiply by 17 on
- d. subtract 17 from

11) Solve the following equation: $A + 17 = 20$

Answer:

- a. $A = -3$
- b. $A = 2$
- c. $A = 3$
- d. $A = 7$

12) To solve $A - 7 = 17$, a person must ? each side of the equation.

Answer:

- a. add 7 to
- b. divide 7 on
- c. multiply by 7 on
- d. subtract 7 from

13) Solve the following equation: $A - 7 = 17$

Answer:

- a. 10
- b. 14
- c. 21
- d. 24

14) Solve the following equation for X: $\frac{(3X)}{3} = \frac{(4 - 1)}{3}$

Answer:

- a. $1 \div 3$
- b. 1
- c. 3
- d. X

15) Solve the following for X: $45X = \frac{120}{2}$

Answer:

- a. $X = 0.075$
- b. $X = 1.33$
- c. $X = 2.667$
- d. $X = 4,050$

16) Solve the following for X: $X - \left(\frac{7}{2}\right) = 120$

Answer:

- a. $X = 60$
- b. $X = 116.5$
- c. $X = -123.5$
- d. $X = 123.5$

17) Solve the following for X: $\frac{128}{X} = 64$

Answer:

- a. $X = 0.2$
- b. $X = 1 \div 2$
- c. $X = 0.75$
- d. $X = 2.0$

18) A(n) ? is a shorthand method for writing a mathematical rule.

Answer:

- a. equal sign (=)
- b. equation
- c. formula
- d. math problem

19) The multiplication of two or more quantities may be expressed as the ? of the same quantities.

Answer:

- a. dividend
- b. product
- c. quotient
- d. sum

20) Division of two quantities is expressed as the ? of those two quantities.

Answer:

- a. dividend
- b. product
- c. quotient
- d. sum

21) ? is expressed as the sum of a given number of quantities.

Answer:

- a. Addition
- b. Multiplication
- c. Subtraction
- d. The square of a number

22) Subtraction is expressed as the ? two quantities.

Answer:

- a. difference between
- b. division of
- c. ratio of
- d. sum of

23) Select the correct Ohm's Law formula that will solve for E when only I and R are known.

Answer:

- a. $E = \frac{I}{R}$
- b. $E = I \times R$
- c. $E = \frac{P}{I}$
- d. $E = \sqrt{P \times R}$

24) Given: $X = Y - 8$, $X = 2 Y$, Solve for X :

Answer:

- a. $X = -8$
 - b. $X = 8$
 - c. $X = -16$
 - d. $X = 16$
- $2 Y = Y - 8$
 $Y = -8$
 $X = 2 \times (-8)$
 $X = -16$

FOR QUESTIONS 25-30 USE THE FORMULAS: $E = I \times R$ AND $P = E \times I$

25) Solve for E when only I and P are known.

Answer:

$$E = \frac{P}{I}$$

26) Solve for E when only R and P are known.

Answer:

$$E = \sqrt{P \times R}$$

27) Solve for R when only E and I are known.

Answer:

$$R = \frac{E}{I}$$

28) Solve for R when only E and P are known.

Answer:

$$R = \frac{E^2}{P}$$

29) Solve for R when only I and P are known.

Answer:

$$R = \frac{P}{I^2}$$

30) Given: $I = 150 \mu\text{A}$ $R = 450 \text{ k}\Omega$, Solve for: E (in volts)

Answer:

- a. 6.75 Volts
- ➔ b. 67.5 Volts $E = 0.000150 \times 450,000$
- c. 675.0 Volts $E = 67.5 \text{ Volts}$
- d. 6,750.0 Volts

31) Given: $R_1 = 10$ $R_2 = 20$ $R_3 = 30$ $I_2 = 5$ $I_3 = 2$

$$100 = I_1 \times R_1 + I_2 R_2 + I_3 R_3$$

Solve for I_1

Answer:

- a. $I_1 = -0.1667$ $100 = 10(I_1) + 20(5) + 30(2)$
- b. $I_1 = 0.1667$ $100 = 10(I_1) + 100 + 60$
- ➔ c. $I_1 = -6$ $100 = 10(I_1) + 160$
- d. $I_1 = 6$ $-60 = 10(I_1)$
- $-6 = I_1 \text{ or } I_1 = -6$

32) Given: $I_N = 10 \text{ Amps}$ $R_N = 2 \Omega$ $R_L = 3 \Omega$

$$I_L = I_N \times \frac{R_N}{R_N + R_L}$$

Solve for I_L

Answer:

- a. $I_L = 0.25 \text{ Amps}$
- ➔ b. $I_L = 4.0 \text{ Amps}$
- c. $I_L = 10 \text{ Amps}$
- d. $I_L = 25 \text{ Amps}$

33) Solve the following equation for HP: $\text{Amps} = \frac{HP \times 746}{E \times \text{Efficiency} \times P_f}$

Method #1

$$\frac{1}{HP} \times \text{Amps} = \frac{\cancel{HP} \times 746}{E \times \text{Efficiency} \times P_f} \times \frac{1}{\cancel{HP}}$$

$$\frac{1}{\cancel{Amps}} \times \frac{\cancel{Amps}}{HP} = \frac{746}{E \times \text{Efficiency} \times P_f} \times \frac{1}{\cancel{Amps}}$$

$$\left(\frac{1}{HP} = \frac{746}{E \times \text{Efficiency} \times P_f \times \text{Amps}} \right)$$

Method #2

$$HP = \frac{E \times \text{Efficiency} \times P_f \times \text{Amps}}{746}$$

$$\frac{\text{Amps}}{1} = \frac{HP \times 746}{E \times \text{Efficiency} \times P_f}$$

$$\frac{E \times \text{Efficiency} \times P_f}{746} \times \frac{\text{Amps}}{1} = \frac{\cancel{HP} \times \cancel{746}}{\cancel{E \times \text{Efficiency} \times P_f}} \times \frac{\cancel{E \times \text{Efficiency} \times P_f}}{\cancel{746}}$$

$$\frac{E \times \text{Efficiency} \times P_f \times \text{Amps}}{746} = HP$$

34) Solve the following formula for P_f : $KW = \frac{E \times I \times P_f \times \sqrt{3}}{1000}$

$$\frac{KW}{1} = \frac{E \times I \times P_f \times \sqrt{3}}{1000}$$

$$\frac{1000}{E \times I \times \sqrt{3}} \times \frac{KW}{1} = \frac{\cancel{E \times I} \times P_f \times \cancel{\sqrt{3}}}{\cancel{1000}} \times \frac{\cancel{1000}}{\cancel{E \times I \times \sqrt{3}}}$$

$$\frac{1000 \times KW}{E \times I \times \sqrt{3}} = P_f$$

35) Solve the following for E_{L-L} : $f = \frac{1.732 \times L \times I_{30}}{C \times E_{L-L}}$

$$E_{L-L} \times f = \frac{1.732 \times L \times I_{30}}{C \times \cancel{E_{L-L}}} \times \cancel{E_{L-L}}$$

$$\frac{\cancel{E_{L-L}} \times f}{\cancel{f}} = \frac{1.732 \times L \times I_{30}}{C \times E_{L-L}} \times \frac{1}{f}$$

$$E_{L-L} = \frac{1.732 \times L \times I_{30}}{C \times f}$$

36) CHALLENGE: solve for R_2 if $R_t = 6$, $R_1 = 12$, $R_3 = 30$ and the following formula is true:

$$R_t = \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right)^{-1}$$

$$\begin{aligned}
 R_t &= \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right)^{-1} \\
 R_t &= \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}} \\
 \frac{R_t}{1} &= \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}} \\
 \left(\frac{R_t}{1} \right) &= \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}} \\
 \frac{1}{R_t} &= \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \\
 \frac{1}{R_t} - \left(\frac{1}{R_1} + \frac{1}{R_3} \right) &= \frac{\cancel{1}}{\cancel{R_1}} + \frac{1}{R_2} + \frac{\cancel{1}}{\cancel{R_3}} - \left(\frac{\cancel{1}}{\cancel{R_1}} + \frac{\cancel{1}}{\cancel{R_3}} \right) \\
 \left(\frac{1}{R_t} - \left(\frac{1}{R_1} + \frac{1}{R_3} \right) \right) &= \frac{1}{R_2} \\
 \frac{1}{R_t} - \left(\frac{1}{R_1} + \frac{1}{R_3} \right) &= R_2 \\
 \left(\frac{1}{R_t} - \left(\frac{1}{R_1} + \frac{1}{R_3} \right) \right)^{-1} &= R_2 \\
 \left(\frac{1}{6} - \left(\frac{1}{12} + \frac{1}{30} \right) \right)^{-1} &= 20
 \end{aligned}$$